Histopathological Image Classification Using Random Binary Hashing Based PCANet and Bilinear Classifier

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Abstract—The computer-aided histopathological image diagnosis has attracted considerable attention. Principal component analysis network (PCANet) is a novel deep learning algorithm with a simple network architecture and parameters. In this work, we propose a random binary hashing (RBH) based PCANet (RBH-PCANet), which can generate multiple randomly encoded binary codes to provide more information. Moreover, we rearrange the local features derived from PCANet to the matrix-form features in order to reduce feature dimensionality, and then we apply the low-rank bilinear classifier (LRBC) to perform effective classification for matrix features. The proposed classification framework using RBH-PCANet and LRBC (RBH-PCANet-LRBC) is adopted for histopathological image classification. The experimental results on both a hepatocellular carcinoma image dataset and a breast cancer image dataset show that the RBH-PCANet-LRBC algorithm achieves best performance compared with other unsupervised deep learning algorithms.

Keywords—PCANet; Random Binary Hashing; Low Rank Bilinear Classifier; Histopathological Image

I. INTRODUCTION

The histopathology based diagnosis remains the “gold standard” for a large number of diseases, including almost all types of cancer. The computer-aided diagnosis (CAD) of histopathological images has attracted much attention.

Feature representation is a critical factor for histopathological image analysis. In recent years, deep learning (DL) has achieved great success for medical images, also including histopathological images [1][2].

Principal component analysis network (PCANet) is a novel DL algorithm, which consists of only three basic components: cascaded PCA as a deep network, binary hashing, and block-wise histograms [3]. Although PCANet has a very simple network architecture and parameters, it indeed achieves excellent performance for image classification compared with other state-of-the-art DL algorithms [3][4]. Moreover, several improved PCANet algorithms have been proposed, such as DLANet [5], SRDANet [6], and SPCANet [7]. However, these variants mainly focus on applying different filters instead of the PCA filter for further improving representation performance.

In PCANet and its variants, the binary hash approach just simply encodes the quantized binary codes according to the sequence of principal components (PC). In other words, the first PC is assigned the most significant bit. However, this simple hashing method cannot provide information rich enough. In fact, the way of binary coding in PCANet also affects representation performance, but it has not been deeply investigated yet.

Random theory based methods, such as the random subspace and random projection algorithms, have been widely used in machine learning. In this work, motivated by the success of random methods, we propose performing random binary hashing (RBH) in PCANet without considering the sequence of PCs, which then generates multiple random binary codes with more information.

Furthermore, the local histogram features extracted from PCANet are usually concatenated to form a feature vector, which has a very high dimensionality resulting in high computational complexity. One solution is to rearrange these local features to a matrix-form, which is then fed to the matrix feature based classifier [8]. The low-rank bilinear classifier (LRBC) is a newly proposed classifier for matrix-form features with outstanding performance [8]. Therefore, it has the potential to generate matrix-form features from PCANet for more effective classification.

In this work, we propose a new classification framework for histopathological images with RBH-based PCANet.
(RBH-PCANet) and LRBC. The main contributions are twofold. First, we propose the RBH-PCANet algorithm to generate more representative information. Second, we rearrange local histogram features derived from RBH-PCANet to matrix-form features, which are then fed to the LRBC algorithm to further improve classification performance for histopathological image based diagnosis.

II. METHODS

Figure 1 shows the proposed classification framework, including RBH-PCANet, spatial pyramid matching (SPM), and LRBC. The RBH-PCANet algorithm is applied to histopathological images to generate local histogram features, which are then pooled and hierarchically re-organized by SPM, because SPM can integrate the spatial information in an image from local block histograms to generate more efficient and compact image feature representation instead of simply concatenated local features [9]. Furthermore, the features from SPM are rearranged to a matrix-form in a new matrix feature space, which are finally fed to LRBC for classification.

A. Cascaded PCA Network

PCANet consists of three basic components: cascaded PCA, binary hashing, and block-wise histograms after binary to decimal conversion (B2DC) [3]. In the first stage of PCA network, a patch with a size of \(m \times n\) is taken for each pixel in \(N\) training images \((I_1)_i\). PCA can be regarded as minimizing the reconstruction error within a family of orthonormal filters, namely

\[
\min_{V \in R^{mn \times L_1}} \|X - VV^T X\|_F^2, \quad \text{s.t.} \quad V^T V = I_{L_1},
\]

where \(X\) is the patch image training set. Then we can achieve \(L_1\) leading components \(q_l\) (\(l = 1, 2, ..., L_1\)) for patches around each pixel in the first layer PCA network. The PCA filters of the first stage are expressed as

\[
W_1^l = mat_{m \times n}(q_l) \in R^{m \times n}, \quad l = 1, 2, ..., L_1
\]

where \(mat_{m \times n}(q)\) denotes a function that maps \(q \in R^m\) to a matrix \(W \in R^{m \times n}\), and \(q_l\) is the \(l\)-th leading eigenvector.

The \(l\)-th filter output of the first stage is given by

\[
\tilde{I}_1^l = I_1 \ast W_1^l, \quad i = 1, 2, ...,\]

where \(\ast\) denotes 2D convolution.

Almost repeating the same process in first stage, the next layer network can be easily built. The PCA filters of the second stage are then obtained as

\[
W_2^l = mat_{m \times n}(q_l^2) \in R^{m \times n}, \quad l = 1, 2, ..., L_2
\]

where \(L_2\) is the number of leading components in the second layer PCA network. For each input \(I_1^l\) of the second stage, \(L_2\) outputs are generated and each convolves \(I_1^l\) with \(W_2^l\)

\[
\theta_1^l = \{I_1^l \ast W_2^l\}^2_{i=1}\,, \quad l = 1, 2, ..., L_2
\]

After filtering by the two-stage cascaded PCA networks, there are \(L_1 \times L_2\) real-valued output images in total. It is worth noting that more PCA stages can be built by simply repeating the above process.

B. Random binary hashing and block-wise histograms

In the original PCANet, a simple binary quantization (hashing) operator is performed on the \(L_1\)-\(L_2\) output images by \(H(I_1^l \ast W_2^l)\), where \(H(\cdot)\) is a function whose value is one for positive entries and zero otherwise [3]. The binary pixel values at the same location are then regarded as an \(L_2\)-bit vector according to the sequence of PCs.

It is worth noting that the current binary hashing operator is one of the \((L_2)^2\) binary codes for \(L_2\)-bit vector; therefore, only limited information is obtained, which affects classification performance.

Motivated by the success of random methods in machine learning, we propose to randomly encode the \(L_2\) binary pixel values \(k\) times without considering the sequence of PCs, which then generate \(k L_2\)-bit vectors. As a consequence, the \(k\) vectors provide more useful information to represent images.

B2DC is then performed after RBH, namely, each \(L_2\)-bit vector is then converted back into a new single integer-valued image:

\[
\tilde{T}_1^l = \sum_{i=1}^{L_2} 2^{i-1} H(I_l^l \ast W_2^l)
\]

Each of the final \(k L_1\) images, it is partitioned into multiple blocks with a size of \(m \times n\), and the decimal values are then counted in each block to yield local histogram features.

C. Spatial Pyramid Matching

An input image generates totally \(k L_1\) images by RBH-PCANet. For the local histogram features, the SPM algorithm is then used for each image to effectively integrate spatial information in image by hierarchical pooling. For detailed algorithm about SPM, readers can refer to [9].

As shown in Fig. 2, the multi-scale pooled local features in different layers of SPM are rearranged to a matrix-form. It should be noted that for \(L_1\) images belonging to the same RBH codes, their local histogram features at the same position are concatenated to form a vector with a dimensionality of \(256 L_1\), which is then processed by SPM to build a 2D matrix of...
features with a size of 256$L_i \times N_\text{s}$, where $N_\text{s}$ is the total number of spatial bins in the multi-level pyramid. In Fig. 2 for example, the first, second and third levels of the pyramid have 16, 4, and 1 bins respectively, and thus $N_\text{s} = 21$. Finally, $k$ feature matrices are generated from $k$ RBH encoding sequences, each with a size of 256$L_i \times N_\text{s}$, and they are connected to form a large matrix with a size of 256$L_i \times (N_\text{s} \times k)$, which serves as the input of LRBC. On the contrast, for a traditional vector-based classifier, features from $N_\text{s}$ bins and $k$ RBH sequences are concatenated to form a large vector of features (Fig. 2).

In this work, $C_\text{w}$ is set by $C_\text{w} = \frac{1}{\|L_\text{w}\|}$, to equally balance the two spectral matrix norms of $I$ and $L_\text{w}$ with $C_h = 1/\|L_\text{h}\|$ for $L_\text{h}$, where $\|L_\text{w}\|$ indicates the spectral matrix norm of $L_\text{w}$. Eq. (9) is then rewritten as

$$\min_{\hat{b}_\text{h}, \hat{b}_\text{w}} \left[ \frac{1}{2} \text{tr} (\hat{M}_\text{w} \hat{M}_\text{w}^T) + \frac{1}{2} \text{tr} (\hat{M}_\text{h} \hat{M}_\text{h}^T) + C \sum_i \max(0, 1 - y_i (\text{tr} (\hat{M}_\text{h}^T \hat{X}_i M_\text{w} + b) )) \right]$$  \hspace{1cm} (10)

where $\hat{X}_i = (I + C_h L_\text{h})^{-1/2} X_i (I + C_\text{w} L_\text{w})^{-1/2}$.

Eq. (10) is the final objective function of the LRBC algorithm, from which we get the smoothed classifier weights $M_\text{h} = (I + C_h L_\text{h})^{-1} \hat{M}_\text{h}$ and $M_\text{w} = (I + C_\text{w} L_\text{w})^{-1/2} \hat{M}_\text{w}$. More detailed optimization solutions and other information about LRBC can be found in [8].

### III. EXPERIMENTS AND RESULTS

#### A. Experiments

Two histopathological image datasets, namely a hepatocellular carcinoma (HCC) image dataset and a breast cancer image dataset, are used in this work. There are 66 HCC images with a size of 1024×768, including 21 well differentiated HCC, 23 moderately differentiated HCC and 22 poorly differentiated HCC [11]. The breast cancer image dataset consists of 20 ductal carcinoma in situ (DCIS) images and 31 usual ductal hyperplasia (UDH) images from the Beth Israel Deaconess Medical Center dataset with a size of 1444×901 [12]. Typical examples are shown in Fig. 3. Here the color images are transformed into grayscale images for feature extraction and image classification.

RBH-PCANet is compared with PCANet, sparse coding (SC) [10], and two commonly used unsupervised DL algorithms, namely stacked auto-encoder (SAE) and deep belief network (DBN) [13]. For fair comparison, both SAE and DBN are set with three-layer networks. The parameters in all the DL algorithms are selected to achieve the best performance. The LRBC algorithm is compared with the linear support vector machine (SVM) classifier.

For each dataset, 10000 patches are randomly sampled from the training set to learn feature representation models for all algorithms. The patch sizes are 17×17 and 11×11 pixels for HCC images and breast images, respectively. The local patches are densely sampled without overlapping for SPM in each image. The leave-one-out strategy is used to evaluate the classification performance. We repeat the above experiments five times to calculate the averaged results.

In RBH-PCANet, the parameters are empirically set as follows: $k = 4$, $L_1 = 8$, $L_2 = 8$ and $N_\text{s} = 21$.

#### B. Results

Table 1 shows the classification results of different algorithms on HCC image dataset. It can be seen that RBH-PCANet is significantly superior to PCANet ($p$-value < 0.05), while PCANet outperforms SC, DBN and SAE. Moreover, the LRBC algorithm also significantly improves the classification performance compared with the feature-vector
based SVM ($p$-value < 0.05). The proposed RBH-PCANet-LRBC algorithm achieves the best results, whose classification accuracy (ACC), sensitivity (SEN) and specificity (SPE) are 95.45±1.07%, 97.38±1.02% and 98.04±0.67%, respectively.

Our method is superior to all other algorithms with a classification accuracy of 94.54±2.03, 94.52±2.09, 97.29±1.03 for the RBH-PCANet-LRBC algorithm respectively, which shows a similar tendency to those based SVM ($p$-value < 0.05). The proposed RBH-PCANet-LRBC algorithm achieves the best performance for diagnosis of histopathological images, which suggests that RBH-PCANet-LRBC has the potential for histopathology-based CAD systems.

The computational load of RBH-PCANet-LRBC for the binary hashing and block-wise histograms is $k$ times that of PCANet. However, the convolution operation in both methods is the most time-consuming, and its computing time is the same for both methods. Hence in total, RBH-PCANet-LRBC is barely inferior to PCANet in terms of computational complexity.

We transform color histopathological images to grayscale images for feature extraction and image classification. Indeed, color information is also important for the histopathology based diagnosis. Future work will be focused on effectively exploring intra-correlations among multiple color channels and fusing information from multi-channels.

### REFERENCES


