CONTOUR DETECTION BY SURROUND INHIBITION
IN THE CIRCULAR HARMONIC FUNCTIONS DOMAIN

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ABSTRACT
Standard edge detectors react to all not negligible luminance changes in an image, irrespective whether they are originated by object contours or by texture (e.g. grass, foliage, waves, etc.). Texture edges are often stronger than object contours, thus standard edge detectors fail in isolating object contours from texture. We propose a multiresolution contour detector, operating in the Circular Harmonic Function domain and motivated by biological principles. At each scale, texture is suppressed by using a bilateral surround inhibition process, applied after non-maxima suppression. The binary contour map is obtained by a contour-oriented thresholding algorithm, proved to be more effective than the classical hysteresis thresholding used in the Canny edge detector. Robustness to noise is achieved by a Bayesian gradient estimation.

1. INTRODUCTION
The last two decades have seen a flourishing development in the field of edge detection. Examples of edge detectors are operators incorporating linear filtering [1], local orientation analysis [2], fitting of analytical models to the image data [3], and local energy [4]. In object recognition tasks, these methods suffer the drawback of reacting to all luminance changes, irrespective of their origin: object contours or texture. Moreover, in many cases the gradient magnitude is stronger on textured areas than on object contours. Since the Human Visual System (HVS) can easily make such a distinction, we take into account some aspects of the HVS to improve the mentioned selectivity property of the contour extraction.

For instance, psychophysical studies show that the HVS processes low and high spatial frequencies with different latencies [5]: low frequencies are processed in the first 0.1 ÷ 0.3s after an image is projected on the retina, thus only the general morphology is perceived; in the subsequent stage, also the information in higher spatial frequencies is processed and details are perceived. This suggests that contour detection should be performed in a multiresolution framework [6], [7].

Other psychophysical and neurophysiological studies reveal the existence of a phenomenon called surround suppression — see e.g. [8], [9] and the references therein — leading to reduction of the response of an orientation selective neuron to an oriented stimulus, when it is surrounded by other similar stimuli. In [9] it is suggested that the biological utility of surround suppression is contour enhancement in natural images rich in background texture. Contour detection becomes an even more challenging task when applied to noisy images. To make contour detection robust to noise, we introduce a Bayesian denoising step that deploys the optimal Minimum Mean Square Error (MMSE) estimator of the gradient in additive noise. According to recent statistical studies on natural images [10], parametric probabilistic models based on Gaussian Scale Mixtures (GSM) are adopted for both signal and noise edge features. This assumption leads to a closed form of the estimator.

In this paper we combine multiresolution analysis, optimal Bayesian MMSE estimation of the gradient, and surround suppression. For multiresolution analysis we use Circular Harmonic Functions (CHF) [11]. The image contours are extracted at different resolutions and the obtained binary maps are combined by the logic AND operator. This approach relies on the assumption that contours are present at each resolution, while texture details are present only at the finest ones. In order to counteract the effect of noise, at each scale we perform noise reduction by using an optimal Bayesian MMSE estimation of the gradient, followed by a biologically motivated surround inhibition step.

2. CIRCULAR HARMONIC FUNCTIONS
In this Section, CHFs are introduced and some considerations on their relevance in modelling some aspects of the early stages of the HVS are detailed. Given an image \( I(x,y) \in L^2(\mathbb{R}^2) \), let \( I_r(r,\theta) = I(\xi_1 + r \cos \theta, \xi_2 + r \sin \theta) \) be its representation in a polar coordinate system \( (r,\theta) \), centered at point \( (\xi_1, \xi_2) \), where \( r = \sqrt{(x-\xi_1)^2 + (y-\xi_2)^2} \) and \( \theta = \arctan \frac{y-\xi_2}{x-\xi_1} \). Then, given a weighting function \( w_{RTP}(r) \), the radial tomographic projection (RTP) is defined as follows:

\[
RTP_r(\xi_1, \xi_2) = \frac{1}{\theta} \int_{0}^{\theta} w_{RTP}(r) I_r(r,\theta) dr
\]

(1)

Since \( RTP_r(\xi_1, \xi_2) \) is periodic with respect to \( \theta \) it can be decomposed into a Fourier series as follows:

\[
RTP_r(\xi_1, \xi_2) = \sum_{n=-\infty}^{\infty} RTP^{(n)}(\xi_1, \xi_2)e^{in\theta}
\]

(2)

with

\[
RTP^{(n)}(\xi_1, \xi_2) = \frac{1}{2\pi} \int_{0}^{2\pi} RTP_r(\xi_1, \xi_2)e^{-in\theta} d\theta
\]

(3)

being the \( n \)-th radial coefficient of the RTP. The radial coefficient...
The functions \( \psi^{(n)}(r, \theta) = h_{\sigma}(r)e^{-j\theta n} \) are known in the literature as circular harmonic functions (CHFs) of order \( n \) with radial profile \( h_{\sigma}(r) \). The CHFs transform generates complex images, where the magnitude reveals the presence of specific features, and the phase is proportional to their orientation. In general, the \( n \)-th order CHF is tuned to the fundamental harmonics of \( n \)-fold angular symmetric patterns, corresponding to edges (\( n = 1 \)), lines (\( n = 2 \)), forks (\( n = 3 \)), and so on. It is worth noting that the polar separability property that characterizes the circular harmonic filters in the spatial domain holds also in the frequency domain.

For the application pursued in this paper, let us consider the following polar separable functions:

\[
\psi^{(n)}(r, \theta) = \left( \frac{r}{\sigma} \right)^{n} e^{-j\theta n} \]

known as “marginal” Hermite filters (\( n = 0,1,2,3,... \)).

Fig. 1 shows the outputs of the “marginal” Hermite filters for a synthetic test image and demonstrates the CHFs’ abilities to highlight edges, lines, forks, and crosses when using the orders \( n = 1,2,3 \), and \( n = 4 \), respectively. For the purpose of this study, in the following we use only CHFs of order \( n = 1 \).

### 3. MULTIRESOLUTION CONTOUR DETECTOR

As well known from multiresolution analysis [11], the outputs of coarse scale edge detectors do not contain much texture (Fig. 2a), but contours are smoothed and shifted [12] and non-maxima suppression destroys the junctions. At fine scales, contours are well detailed (Fig 2b), but much texture is present. The advantages given of different resolutions can be exploited by selecting, from the binary edge map obtained at a fine scale, only those edge pixels being close enough to edge pixels present in a map obtained at a coarse scale (Fig. 2c).

We apply this principle to the binary outputs of \( N \) Scale Dependant Contour Enhancers (SDCE) each of which is responsible for a different resolution (Fig. 3). The design of a SDCE is described in Section 4.

Specifically, let us consider a given image \( I(x,y) \) and its observed version \( \tilde{I}(x,y) \) corrupted by additive independent observation noise \( Z(x,y) \). First, the noisy image undergoes a multiresolution analysis by taking the magnitudes of the results of convolutions with CHF functions \( \psi_{\sigma_{i}}^{(1)}(x,y) \) of order \( n = 1 \) of different resolutions \( \sigma_{i} \), \( i = 0,1,...,N-1 \):

\[
I_{\sigma_{i}}^{(1)}(x,y) = |\tilde{I}(x,y) \ast \psi_{\sigma_{i}}^{(1)}(x,y)| .
\]

Then binary maps \( h_{k} \) are computed by applying the SDCE operator described in Section 4:

\[
b_{k} = SDCE_{\sigma_{i}}(I_{\sigma_{i}}^{(1)})
\]

The binary maps obtained at different scales are combined as shown in Fig. 3. First, we apply morphological dilation to all binary maps but the one that corresponds to the finest scale:

\[
b_{\text{m}} = b_{k} \odot D_{\sigma}, \quad k = 2,...,N-1
\]

where we use a disk \( D_{\sigma} \) of radius three pixels as a structuring element. The final output is given by the logic AND of the binary maps at all resolutions:

\[
b_{\text{m}} = b_{k}(x,y) \prod_{k=1}^{N-1} b_{k}(x,y)
\]

Morphological dilation compensates the shifting at the coarser resolutions and restores the junctions.

### 4. SCALE DEPENDANT CONTOUR ENHANCER

The proposed Scale Dependant Contour Enhancer (SDCE) is depicted in Fig. 4. The first processing step is Bayesian denoising (Section 4.1). Then non-maxima suppression and surround inhibition are performed (Section 4.2), followed by binarization (Section 4.3).

#### 4.1 Bayesian denoising

Our goal is to find the optimal estimator \( \hat{I}_{\sigma} = \hat{a}(z) \) for the unknown vector \( a = I_{\sigma} \), when a noisy version \( z = I_{\sigma} + Z_{\sigma} \) is observed. As well known from the Bayesian estimation theory, the MMSE estimator is given by:

\[
\hat{a}(z) = \frac{p_{a|z}(z|a)p_{a}(a)}{\int p_{a|z}(z|a)p_{a}(a)da}
\]

### Figure 2 - Binary maps obtained from the outputs of a CHF filter for: (a) a coarse scale, (b) a fine scale, (c) a combination of the two scales by morphological dilation and logic AND.

![Figure 2 - Binary maps obtained from the outputs of a CHF filter](image-url)

### Figure 3 – Multiscale contour detector.

![Figure 3 – Multiscale contour detector](image-url)

### Figure 4 - Single scale contour detector.
According to recent statistical studies on natural images [11], both $p_s(a)$ and $p_p(z|a)$ are assumed Gaussian, with covariance matrices $A_s$ and $A_p$ for the signal and the noise, respectively:

$$p_s(a) = \sum_{i=1}^{K_s} \lambda_i N_s(a, 0, A_s), \quad \sum_{i=1}^{K_s} \lambda_i = \sum_{i=1}^{K_r} \beta_i = 1 \quad (12)$$

where:

$$N_s(\xi, \mu, R) = \frac{1}{2\pi \det R} \exp \left[ -\frac{1}{2} (\xi - \mu)^T R^{-1} (\xi - \mu) \right] \quad (13)$$

By substituting eq. (12) in eq. (11), we can find the following closed expression for the optimal MMSE estimator:

$$\hat{a}(z) = \frac{\sum_{i=1}^{K_s} \lambda_i N_s(z, 0, A_s + N_s) A_s (A_s + N_s)^{-1} z}{\sum_{i=1}^{K_s} N_s(z, 0, A_s + N_s)} \quad (14)$$

The nonlinearity defined by eq. (14), applied to each pixel of $I^r$, gives the optimal MMSE estimation $\hat{I}_s$ of $I_s$. It is worth pointing out that the best linear MMSE estimate would give the Wiener filter.

### 4.2 Surround inhibition

Next, surround inhibition reduces the strength of those edges which are surrounded by other edges. This mechanism is inspired by psychophysical and neurophysiological findings (see [7-9] and references therein). In [7-9] the contour strength is modulated by the positions of neighboring contours. This auto-inhibition is inhibited by other parts of the same contour that fall in the surround inhibition area of the concerned position. This auto-inhibition scheme with respect to [8, 9]. The proposed modifications allow the use of higher values of $\sigma$.

We compute the following two convolutions and take their minimum as an inhibition term:

$$T_s(x, y) = \min \left\{ T_s(x, y), T_s(x, y) \right\} \quad (22)$$

The convolutions are computed for a discrete set of orientations $\phi \in [0, \pi]$, leading to more effective texture suppression.

On isolated edges (Fig. 5a), the local averages on both the sides are very low, ideally zero; consequently, $T_s(x, y)$ is low and contours are not inhibited. On textured areas (Fig. 6a), the local averages on both the sides of an edge are high and similar to each other, thus the inhibition term is high and such texture edges are suppressed. Borders of textured areas are not inhibited, since $T_s(x, y)$ is low on such points (Fig. 5c).

The advantage of performing surround inhibition after the non-maxima suppression is illustrated by Fig. 6. Fig. 6a shows the set $S_o$ of local gradient maxima and we see that the contours of the elephant are well separated from the rest of the texture. Therefore, a half-ring centred on a point of such a contour, and appropriately oriented, contains only a few nonzero pixels and the corresponding inhibition term $T_s(x, y)$ will be extremely small. By comparing Figs. 6b and 6c we can see the improvement achieved by the proposed inhibition scheme with respect to [8, 9]. The proposed modifications allow the use of higher values of $\alpha$, leading to more effective texture suppression.

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**Figure 5** - Half-rings on which $M_s(x, y)$ is averaged, for: (a) isolated edges, (b) textured areas, and (c) borders of textured areas.

**Figure 6** - (a) Set $S_o$ for the test image “Elephant”. (b, c) Contours obtained with the inhibition schemes proposed in this paper (b) and in [9] (c).
suppression, without affecting object contours.

4.3 Binarization

Similar to other methods for edge and contour detection, the last step of the algorithm comprises binarization by thresholding. One well known problem with traditional thresholding techniques, such as global or hysteresis thresholding [1], is that they cannot deal with the quite common situation of weak contours. The gradient magnitude at such contours is smaller than at spurious edges originated by noise or texture. In this paper, we present a new thresholding algorithm, based on the observation that contours lead to long connected components of nonzero pixels, while texture edges lead to relatively short and thin components.

Let \( \{ C_{k}^{(a)} \}_{k=1}^{N} \) be the connected components of \( S_{a} \) (eq. 15), i.e.:

\[
S_{a} = \bigcup_{k} C_{k}^{(a)}
\]

(23)

For each connected component \( C_{k}^{(a)} \), we introduce a quantity \( R_{k}^{(a)} \), we call contour weight, defined as the sum of the values of \( c_{a}(x,y) \) over \( C_{k}^{(a)} \):

\[
R_{k}^{(a)} = \sum_{(x,y) \in C_{k}^{(a)}} c_{a}(x,y)
\]

(24)

We define a binary map \( b_{a} \) as the union of all connected components \( C_{k}^{(a)} \) whose weight \( R_{k}^{(a)} \) is above a given threshold \( \gamma_{c} \):

\[
b_{a} = \bigcup_{k} C_{k}^{(a)} \quad \text{with} \quad R_{k}^{(a)} > \gamma_{c}
\]

(25)

By comparing eqs. (23) and (25) we can see that \( b_{a} \subseteq S_{a} \), where all components \( C_{k}^{(a)} \) which do not correspond to any meaningful contour have been removed (Figs. 6a, 6b).

On a weak edge, like the contour of the hill in Fig. 9a, the gradient magnitude \( M_{a}(x,y) \) is very low and it would (partially) not be detected by a standard binarization technique. However, since the contour of the hill forms a long chain of connected components, its magnitude at such contours is smaller than at spurious edges originated by noise or texture. The dissimilarity between the ground truth and the output of a given operator defined as follows:

\[
\rho = \frac{\sum_{i} \gamma_{i} E_{i}}{\sum_{i} (E_{i} + MP_{i}) + RT}
\]

(25)

where \( AR \) (Algorithmic Result) is the set of 1-pixels detected by a given algorithm, \( \gamma_{i} \) indicates the number of pixels of the set \( X \) and \( X \) indicates the complementary set of \( X \). \( MP_{i} \) is the number of correctly detected contour pixels, i.e. the pixels present both in the result and in the ground truth. \( MP_{i} \) is the number of false negatives, i.e. points which are present in the ground truth but not in the operator output. \( RT \) is the number of points present in the \( AR \) but not in the ground truth and gives a measure of unsuppressed texture.

The values of \( \rho \) for the considered algorithms are presented in Fig. 12, where we can see that the proposed approach outperforms both standard techniques and more sophisticated algorithms based on single and multiscale surround inhibition.

6. CONCLUSIONS

The proposed multiscale contour detector, operating in the CHF domain, discriminates object contours from texture. At each scale, texture is suppressed by a biologically motivated surround inhibition step, where auto-inhibition is avoided by (i) the bilateral computation scheme of the inhibition term and (ii) the application of the inhibition after the non-maxima suppression. This allows to use a larger value of the inhibition coefficient and leads to more effective texture suppression.

![Image 11](a) Original image (a) and its multiset ground truth (b).

![Image 12](a) Noisy images

![Image 12](b) Values of \( \rho \) for the studied algorithms, both for noiseless and noisy images.)
Binary contour maps are obtained by thresholding the weight assigned to each connected contour component. This leads to better results than pixel-wise thresholding of the gradient magnitude $M_\sigma$ because long weak edges are preserved. Robustness to noise for the general non-Gaussian case is achieved by using a Bayesian estimator. GSM models are employed for both the image and the noise and a closed form of the estimator has been provided.

As shown by the experimental results and performance evaluation, our algorithm outperforms both standard and more sophisticated approaches.

REFERENCES


Figure 7 - (a) Input image “Elephant” and contours detected with: (b) the proposed approach, (c) the Canny edge detector, (d) the multiscale edge detector CARTOON without surround inhibition [6], (e) single [9] and (f) multi scale surround inhibition [7].

Fig. 10. Contours detected on the noisy image test (SNR = 13dB)

Figure 9 - (a) Input image “Rino” and contours detected with: (b) the proposed approach, (c) the Canny edge detector, (d) the multiscale edge detector CARTOON without surround inhibition [6], (e) single [9] and (f) multi scale surround inhibition [7].

Fig. 18. Contours detected on the noisy image test (SNR = 13dB)