FAST ALGORITHM FOR IMAGE DATABASE INDEXING BASED ON LATTICE

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ABSTRACT
Extracting feature vectors from images has been largely investigated in the literature. In contrast, browsing the image databases has not been as much studied. We propose a new efficient method for indexing a large amount of feature vectors in high dimensional space. For that purpose, we introduce a new organization of the feature vectors based on the lattice vector quantization and indexing.

1. INTRODUCTION
Along with the rapid development of multimedia devices and the internet, the amount of images has been dramatically increased in the past decade. Content-Based Image Retrieval (CBIR) [1] has mainly focused on using primitive features such as color, texture, shape, etc., for describing and comparing visual contents. But, the growth of the number of images in the database and the dimensionality of the computed feature vectors are the two major handicaps to provide efficient access to the images of the database. Therefore it is essential to use appropriate indexing techniques to search in the high dimensional feature space. Indexing techniques such as Kd-tree [2], R-trees [3], SS-trees [4] are used to realize fast search in the high dimensional feature space. These structures perform better than the scan sequential algorithm (SSA) but they are still dependent on both the feature vectors dimensions and the number of images in the database. In this paper we present a new method for speeding up the retrieval in the feature vectors space. The basic principle is as follows: feature vectors are quantized and indexed in a \( \mathbb{Z}^n \) lattice. Fast retrieval is achieved by using the good properties of the lattice. The paper is organized as follows. In section 2, we describe some indexing techniques from the literature to organize the feature vectors. In section 3, we present the adapted method to extract a fuzzy descriptor based on the combination of different wavelet basis. In Section 4 we describe the algorithm used to index a given feature vector. In section 5, we propose our browsing method to speed up the image retrieval process. In Section 6 we present some simulation results. We finally conclude in section 7.

2. RELATED WORKS
In many applications, indexing high-dimensional data has become increasingly important. In image databases, for example, the images are usually mapped to feature vectors in some high-dimensional space and queries are processed against a database of those feature vectors. The simplest method to realize similarity search is the sequential scan algorithm (SSA). Every feature vector in the database is scanned to find if it satisfies the query requirement. So, SSA depends on the number of images in the database and on the dimensions of the feature vectors. There are a lot of methods to organize the feature vectors of images in the database such that a ranked list of nearest neighbors can be retrieved without performing an exhaustive comparison with all the database image feature vectors. The state-of-the-art works done on indexing high-dimensional vectors focused mainly on two different approaches.

The first approach is based on a number of statistical algorithms such as principal component analysis [5], and latent semantic analysis [6]. These techniques are based on the observation that feature vectors in high-dimensional space are highly correlated and clustered. These methods of feature space reduction try to identify patterns in the feature space by expressing them in such a way to highlight differences and similarities that exist between feature vectors. Once these patterns are found the data can be compressed reducing the number of dimensionality. The major inconvenience of these approaches is that in many cases we will have the risk of loss of the pertinent information in the feature space resulting from the reduction of the dimensionality. The second approach is based on a number of index structures such as Kd-tree [2], R-trees [3] and SS-trees [4]. Unfortunately, currently available index structures for spatial data do not adequately support an effective indexing of more than five dimensions. The query performance of these structures degrade rapidly when the dimension of the feature vectors increases. In [7] the authors report that the query performances degrades by a factor of 12 as the dimensionality increases from 5 to 10. The major problem of the indexing structures based methods is the overlap of the bounding boxes that cover the space of the multidimensional vectors with the query window, which increases with the dimensions.

3. FEATURE VECTOR EXTRACTION

3.1 Low level feature extraction
In this section, we present the method used to extract the feature vectors. We use the wavelet transform to extract the color information. We firstly decompose the image to its individual color components RGB. The commonly used RGB color values do not correspond to human perception of color and hence are not preferred for problems like content retrieval. So we convert the images to the CIE-Lab space. Then, we use a set of orthogonal and biorthogonal discrete wavelets to transform each color component of the image in the spatio-frequency domain which is more representative than the spatial domain. We apply for that a wavelet transform with \( l = 5 \) levels of decomposition on each component of the CIE-Lab color space. We compute the standard deviation of the coefficients of the five low frequency bands obtained by the decomposition. Then, we extract from each decomposition level a feature vector containing a single coefficient. This greatly reduces the computational complexity of search through large databases since we obtain a \( 3 \times l \) dimensional feature vector from each color space component. Here we obtain a 15 dimensional feature vector which reflects the low frequency information describing the color image properties.

3.2 Fuzzy descriptor extraction
In a first stage, we extract the feature vector of each image in the database using the low level visual descriptor presented in Section 3.1 and group the feature vectors in a feature matrix \( M \). The size of this matrix is \( m \) by \( n \) where \( n \) is the number of coordinates of each feature vector and \( m \) is the number of images in the database.
We use the fuzzy c-means (FCM) \[8\] algorithm to partition each feature vector in the matrix \(M\) of size \(k\), where \(k\) indicates the degree of membership of the feature vector of each image in a cluster. Degrees between 0 and 1 indicate that the feature vector has partial membership in a cluster. The matrix \(U_w\) given by (1) is of size \(N_{\text{cluster}}\) by \(m\):

\[
U_w = \{U_w(j,k), 1 \leq j \leq m, 1 \leq k \leq N_{\text{cluster}}\} \tag{1}
\]

where the coefficient \(U_w(j,k)\) assigned to the row \(j\) and the column \(k\) of \(U_w\) indicates the degree of membership of the \(j^{th}\) image in the \(k^{th}\) cluster. The parameter \(N_{\text{cluster}}\) determines the dimensionality of the feature space \(U_w\). Since, we use in our experiments, as described later in Section 3.2, an image database formed by 8 categories, we set \(N_{\text{cluster}}\) to 8. The advantage of the proposed approach is the reduction of the feature space dimensionality since we obtain a fuzzy feature with \(N_{\text{cluster}}\) coefficients instead of 15 obtained using the low level visual descriptor.

After that, for each \(j^{th}\) image stored in the database, we extract what we call the fuzzy visual image descriptor which corresponds to the \(j^{th}\) row of \(U_w\).

### 3.3 Combining different wavelet basis

We propose to use in this work three different wavelets basis (the Daubechies4, the orthogonal Beta \[9, 10\] and the 9-7 filters \[11\]).

#### 3.3.1 Lattice vector indexing

We use the fuzzy c-means (FCM) [8] algorithm to partition each feature vector in the matrix \(M\) in \(N_{\text{cluster}}\) (the number of clusters). Then, we compute the membership matrix \(U_w\) which contains the degree of membership of the feature vector of each image in each cluster. Degrees between 0 and 1 indicate that the feature vector has partial membership in a cluster. The matrix \(U_w\) given by (1) is of size \(N_{\text{cluster}}\) by \(m\):

\[
U_w = \{U_w(j,k), 1 \leq j \leq m, 1 \leq k \leq N_{\text{cluster}}\} \tag{1}
\]

where the coefficient \(U_w(j,k)\) assigned to the row \(j\) and the column \(k\) of \(U_w\) indicates the degree of membership of the \(j^{th}\) image in the \(k^{th}\) cluster. The parameter \(N_{\text{cluster}}\) determines the dimensionality of the feature space of the feature vector. Since, we use in our experiments, as described later in Section 3.2, an image database formed by 8 categories, we set \(N_{\text{cluster}}\) to 8. The advantage of the proposed approach is the reduction of the feature space dimensionality since we obtain a fuzzy feature with \(N_{\text{cluster}}\) coefficients instead of 15 obtained using the low level visual descriptor.

After that, for each \(j^{th}\) image stored in the database, we extract what we call the fuzzy visual image descriptor which corresponds to the \(j^{th}\) row of \(U_w\).

### 4. INDEXING FEATURE VECTORS

Once the feature vectors are extracted, they must be indexed in such a way that a fast and efficient retrieval in the database is guaranteed. For that purpose, we quantize each feature vector using a lattice vector quantizer (LVQ) and assign the index of the lattice vector to the corresponding feature vector. We propose to use the \(Z^n\) lattice in order to guarantee a fast navigation over the points in the \(n\)-dimensional space and allow a fast correspondence between a lattice vector and its index. More details are given hereinafter.

#### 4.1 Lattice vector indexing

A lattice \(\Lambda\) in \(\mathbb{R}^n\) is composed of all integral combination of a set of linearly independent vectors \(\alpha_i\) (the basis of the lattice) such that:

\[
\Lambda = \{x|x = u_1\alpha_1 + u_2\alpha_2 + ... + u_n\alpha_n\} \tag{3}
\]

where the \(u_i\) are integers. The partition of the space is hence regular and depends only on the chosen basis vectors \(\alpha_i \in \mathbb{R}^n\) (\(m \geq n\)). Note that each set of basis vectors define a different lattice. Such a regular structure permits to identify the nearest vectors in the space using fast algorithms. In the case of image retrieval, since similar images have the smallest euclidian distance between their feature vectors, the use of a lattice should permit to retrieve the most similar images in an efficient way.

The LVQ is an efficient algorithm for finding the closest lattice vector \(x\) of a query feature vector \(v\). In the case of a \(Z^n\) lattice, the closest lattice vector with a precision \(\gamma\) is given by:

\[
x = v \left\lfloor \frac{v}{\gamma} \right\rfloor \tag{4}
\]

where \([\cdot]\) stands for the ‘round’ operator, and \(\gamma\) is a scaling factor. As we will see in Sections 5 and 6 the choice of the scaling factor must be such that a good compromise between efficiency and computational complexity (speed) is achieved.

Once the feature vectors are quantized into lattice vectors \(x\), we may attribute a unique and decodable index for each \(x\). Feature vectors are obtained by the FCM algorithm and thus their coordinates are always positive numbers located in the first octant (as well as their quantized coordinates in the lattice). The proposed indexing method computes an index by classifying the lattice vectors according to their norm and the geometrical properties of the lattice. Actually, taking into account the properties of the feature vectors, an index is composed by a set of indices: an index for the norm (\(I_N\)), an index for the leader (\(I_L\)), and finally an index for the permutation (\(I_P\)). Let us detail each of these indices in the following:

- The index for the norm (\(I_N\)) is given by the \(l_1\) norm \(\|x\|_1 = \sum_{i=1}^{n} |x_i|\) (since the coordinates are positive numbers) of the lattice vector \(x\). It classifies the different lattice vectors \(x\) in different hyper-pyramids (shells);
- The lattice vectors lying on the same shell with index \(I_N\) are subdivided to a few number of vectors, called leaders. The leaders are vectors from which all the other lattice vectors of the corresponding shell can be generated by permutations and sign changes of its coordinates (here, there is no sign changes since all the coordinates are positives). The Section 4.2 explains in details how the leader indices \(I_L\) are computed;
- The index for the permutation (\(I_P\)) is computed by the Schalkwijk algorithm as in [12].

This indexing method creates an hierarchical tree-structure of indices adapted to the database indexing framework (see Section 6).

#### 4.2 Proposed leader indexing

The proposed algorithm classifies all the leader indices in such a way that the indexing is no longer based on a greedy search algorithm or direct addressing, but on low-cost enumeration algorithm which just depends on the quantity of leaders instead of on the explicit knowledge of all of them.

A hyper-pyramid of radius \(r\) and dimension \(n\) is composed by all the vectors \(v\) such that \(\|v\|_1 = r\). As said before, leaders are the elementary vectors of a hyper-surface from which operations of permutations and sign changes lead to all the other vectors lying on this hyper-surface. Indeed, the leaders are vectors with positive coordinates sorted in increasing (or decreasing) order. Therefore, leaders for a \(l_1\) norm are vectors which verify the conditions below:

1. \(\sum_{i=1}^{n} v_i = r\),
2. \(0 \leq v_i \leq v_j\), for all \(i < j\).

In the case of a \(l_1\) norm, one can note that those conditions are linked to the theory of partitions in number theory [13]. Indeed, in number theory a partition of a positive integer \(r\) is a way of writing \(r\) as a sum of \(d\) positive integers (also called \(\text{part}\)). The number of partitions of \(r\) is given by the partition function \(p(r)\) such that:

\[
p(r) = \sum_{r=0}^{\infty} p(r) = \prod_{d=1}^{\infty} \left(1 + \frac{1}{1-x^d}\right). \tag{5}
\]
which corresponds to the reciprocal of the Euler’s function $\gamma$ \cite{13}. Further mathematical development lead to representations of the $p(r)$ function that allow faster computation. Interested readers should refer to \cite{13}.

However, we are usually interested in shells of $l_1$ norm equals to $r$ in a $d$-dimensional lattice with $r \neq 0$. In this case, one can use the function $q(r,d)$ \cite{13} which computes the number of partitions of $r$ with at most $d$ parts (in partition theory it is equivalent to the number of partitions of $r$ with no element greater than $d$ with any number of parts). Then, for a hyper-pyramid of norm $r = 5$ and dimension $d = 3$, we have $q(5,3) = 5$, i.e., five leaders given by: $(0,0,5), (0,1,4), (0,2,3), (1,1,3),$ and $(1,2,2)$.

The function $q(r,d)$ can be computed from the recurrence relation\cite{13}:

\[ q(r,d) = q(r,d-1) + q(r-d,d) \]

with $q(r,d) = p(r)$ for $d > r$, $q(1,d) = 1$ and $q(0,0) = 0$.

4.2.1 Using function $q(r,d)$ to index the leaders

As we will see in the following, Equation (6) not only gives the total number of leaders with the largest coordinate equal to $x$ using the function $q(r,d)$, but also the number of leaders with largest coordinate equal to $x$ with dimension $d$. Clearly, computing the number of leaders with the largest coordinate equal to $x$ with norm $r$ and dimension $d = n$, is equivalent to calculate the number of leaders of norm $r = (x_n + 1)$ with dimension $n + 1$.

By introducing the function $\gamma(r,d,k)$ given in Appendix, which counts all the partitions of a number $r$ with at most $d$ parts not greater than $k$, we can show that the index of a leader can be computed using the following formula:

\[ I_L = \sum_{j=0}^{n-2} \min_{i=0}^{x_n} \sum_{i=x_n+1}^{\min[x_p(j+1),r_n]} \gamma(r_n-j-i,n-(j+1),i) \]

where $x_{n+1} = +\infty$ and $q(0,d) = 1$. Note that, when $r_n-j-i$ is less than or equal to $i$, $\gamma(r_n-j-i,n-(j+1),i) = q(r_n-j-i,n-(j+1))$, because in that case all vectors counted by $q(r,n)$ are leaders.

5. PROPOSED METHOD

5.1 Principle of the method

Lattice vector quantization based on $Z^n$ divide the data space into hypercubes. The centroid of each hypercube is a lattice point. Each feature vector of the feature space $F_s$ obtained as explained in Section\ref{section3.3} is quantized in a lattice point. The query procedure is given as follows:

1. The query feature vector is computed;
2. The query feature vector is quantized in a lattice point;
3. We exploit the good properties of the lattice space to determine the nearest lattice points of the quantized query feature vector;
4. We collect the images of the database quantized by the nearest lattice points;
5. We perform SSA on the feature vectors of the collected images.

All these steps are described in the following sections.

5.2 Building the search tree

The obtained feature space $F_s$ computed as explained in Section\ref{section3.3} is quantized using a scaling factor $\gamma$:

\[ G_w = \left[ \frac{F_w}{\gamma} \right] \]

where $[.]$ stands for the ‘round’ operator. Then, each quantized feature vector is indexed with the indices of norm, leader and permutation as explained in Section\ref{section4}. The search tree is built as presented in Figure\ref{fig1}. It has four levels. In the first three levels, each level contains a certain number of hash tables. Each hash table has a given number of buckets, each bucket contains one key and one node. In the fourth level, each leaf node contains a list of images indexed in the same lattice point. In the root of the tree, we construct the hash table $H_{root}$ associated to the index of norm $I_N$. If two images have the same $I_N$ they are associated to the same bucket in $H_{root}$. The key in each bucket of $H_{root}$ is the index of norm of the quantized feature vectors of the images existing in the database. The child of the node that exists in the bucket of $H_{root}$ containing the key $I_N$, is the hash table $Child_L$. The keys of each bucket of $Child_L$ are the indices of leaders $I_{L_{ij}}$ of the quantized feature vectors of the images existing in the database that have the same index of norm $I_N$. The child of the node that exists in the bucket of $Child_L$ containing the key $I_L$, is the hash table $Child_P$. The keys of $Child_P$ are the indices of permutation $I_P$ of the quantized feature vectors of the images existing in the database that have the same $I_N$ and the same $I_L$. The child of the node that exists in the bucket of $Child_P$ containing the key $I_P$, is a leaf node $Leaf_{I_N,I_L,I_P}$ containing the list of images existing in the database that have the same indices of norm, leader and permutation corresponding respectively to $I_N$, $I_L$ and $I_P$. For example, in Figure\ref{fig1} the keys of the Hash table $Child_L$ are the indices of leader of images in the database having the same index of norm 9. The keys of $Child_P$ are the indices of permutation of images in the database having the same indices of norm and leader corresponding respectively to (9,5). The images located in the leaf node $Leaf_{I_N=9,I_L=5,I_P=6}$ are image1 and image3.

![image](image1)

![image](image2)

![image](image3)

![image](image4)

![image](image5)

Table 1: The indices of norm, leader and permutation of each image presented in the search tree of Figure\ref{fig1}.

5.3 Retrieving the $k$ nearest images

We implemented an image retrieval system with the Java language using Apache Tomcat server. The system allows the user to bring the query image in existing pictures from the hard disk, the web or drawings constructed on any other drawing tools.

Let us first define the nearest neighbor lattice vectors $x$ of the
To retrieve the images quantized by the same lattice vector \( \mathbf{v} \) we proceed as follows. We compute the index of norm \( \mathbf{v} \) of the lattice vector \( \mathbf{v} \) as\(^2\):

\[
\text{mask}_p = \left\{ \mathbf{x} \in \Lambda, \sum_p x_p^2 = p, p \in \mathcal{P} \subset \mathbb{N} \right\}
\]

which defines the lattice vectors at the square distance \( p \) from the origin. For example, as showed in Figure 2 for a lattice \( \mathbb{Z}^2 \), the neighbors at a square distance \( p = 4 \) from the origin of the lattice are given by \( \text{mask}_4 = \{ (0,2), (2,0), (2,2), (0,0) \} \). They correspond to the third neighborhood of the null vector \( \mathbf{0} \).

The proposed basic procedure to retrieve the \( k \) nearest images of query image is given by the following steps:

1. A combined fuzzy color feature vector is extracted from the query image and quantized by the lattice vector \( \mathbf{v}_{\text{query}} \);
2. Retrieve in the database all the images quantized by the lattice vector \( \mathbf{v}_{\text{query}} \) as described in Section 5.4;
3. If the number \( k_1 \) of images in the database quantized by \( \mathbf{v}_{\text{query}} \) is at least equal to \( k \), then go to step 6 else go to step 4;
4. The set \( E \) of lattice vectors corresponding to the neighbors of \( \mathbf{v}_{\text{query}} \) up to a maximum square distance \( P \) is defined by:
   \[
   E = \left\{ E_1, E_2, ..., E_P \right\} \quad \text{for } p \in \mathcal{P}
   \]
   with,
   \[
   E_p = \{ \mathbf{v} \in \Lambda, \mathbf{v} = \mathbf{v}_{\text{query}} + \mathbf{x}, \mathbf{x} \in \text{mask}_p \};
   \]
5. Retrieve the \( k_2 \) database images quantized by vectors of \( E \) (satisfying \( k_1 + k_2 \geq k \)). This step is described in Section 5.4;
6. Performs the SSA on the \( k_1 \) or \( k_1 + k_2 \) database images and return the \( k \) nearest images to the query vector;
7. Exit.

5.4 Retrieving the database images

To retrieve the images quantized by the same lattice vector \( \mathbf{v} \), we proceed as follows. We compute the index of norm \( I_{\mathbf{v}} \) of the quantized feature vector \( \mathbf{v} \). We search \( I_{\mathbf{v}} \) in the root hash table \( H_{\text{root}} \). If it does not exist, we exit the search process without returning any images. If \( I_{\mathbf{v}} \) exists, we compute the leader index \( I_{\mathbf{v}}^L \) of \( \mathbf{v} \) and we search \( I_{\mathbf{v}}^L \) in \( \text{Child}(I_{\mathbf{v}}) \). If \( I_{\mathbf{v}}^L \) does not exist, we exit the search process without returning any images. If \( I_{\mathbf{v}}^L \) exists, we compute the permutation index \( I_{\mathbf{v}}^P \) of \( \mathbf{v} \) and we search \( I_{\mathbf{v}}^P \) in \( \text{Child}(I_{\mathbf{v}}^L) \). If it does not exist, we exit the search process without returning any images. If \( I_{\mathbf{v}}^P \) exists, we take from the leaf node \( \text{Child}(I_{\mathbf{v}}^L,I_{\mathbf{v}}^P) \) the images indexed by the same indices of norm, leader and permutation \(( I_{\mathbf{v}}^N, I_{\mathbf{v}}^L, I_{\mathbf{v}}^P )) \) as the quantized feature vector \( \mathbf{v} \).

\(^2\)This operation is done off-line.

5.5 Advantages of the proposed method

One advantage of the proposed retrieval method is that it is adapted to image databases that have an important number of images. Indeed, if we increase the number of images in the database, we obtain a lattice space more dense, consequently more useful for indexing. Besides, to search the images quantized in a given lattice point located at the neighborhood of \( \mathbf{v}_{\text{query}} \), we search at most only in three levels of the tree independently of the dimension of the feature space. Indeed, we parse the all three levels only if there are images in the database that are quantized in this given lattice point. Another advantage is that the speed up can be improved selecting the optimal scaling factor. If it is small then the source is expanded and the lattice will be less dense. Then, for retrieving a certain number of images the retrieval engine has to parse an important number of nearest lattice points and the speed up cost will be more important. If the scaling factor is great the source is contracted, the lattice will be very dense so the retrieval window increases but the speed up is degraded because we must perform SSA on a large number of images. So we have a trade off between the number of images in which the SSA is applied and the number of the browsed lattice points located at the neighborhood of \( \mathbf{v}_{\text{query}} \). To realize this trade off our solution consists on varying the scaling factor and selecting experimentally the optimal scaling factor.

6. SIMULATION RESULTS AND DISCUSSION

We conducted our tests on a subset of the COREL database, formed by 8 image categories (Horses, Flowers, Buildings, Buses, Dinosaurs, Elephants, Mountains and glaciers, Lights) each containing 100 images. The images are translated scaled and rotate to obtain an image database containing 40000 images. Experiments were performed on a personal computer with configurations: Intel Pentium M 725 (1.6 GHZ), 512 MB memory DDR 333 MHz, 80 GB HDD. We have tested the performance of our proposed image retrieval method taking into account both the classical precision measures (the ratio between the number of images returned belonging to the same category as the query and the number of images required by the user) and the speed-up of the retrieval process. The dimension of the feature vectors that we used in our experiments is equal to 24, since we have combined three feature vectors each one extracted from a different wavelet basis (Daubechies4, Beta and 9/7 filters). We have used three different scaling factors (1/2, 1/3 and 1/4) and three different ranks (8, 60 and 200). The rank is the number of images required by the user. We define the speed-up parameter as:

\[
\text{speed-up} = \frac{t(\text{SSA})}{t(\text{indexing})}
\]

where \( t(\text{SSA}) \) is the elapsed time for SSA method and \( t(\text{indexing}) \) is elapsed time for the Kd-tree or the proposed retrieval method. Note that all feature vectors as well as the built trees of the proposed method and Kd-tree should be resident in the main memory when evaluating \( t(\text{SSA}) \) and \( t(\text{indexing}) \). So the speed-up is mainly dependant on computational complexity, i.e. CPU cost. We have found experimentally that for the scaling factors (1/2, 1/3 and 1/4),
we obtain best performances than the Kd-tree in terms of time spent on the retrieval process for all used k (number of nearest neighbors to be retrieved) (see Tables 2 and 3). We present in Table 2 a comparison between the retrieval speed-up of the retrieval method based on lattice using the scaling factor 1/3 and the k-d-tree.

Table 2: Speed-up comparison between the proposed indexing method and the Kd-tree.

<table>
<thead>
<tr>
<th>k</th>
<th>Kd-tree</th>
<th>Lattice</th>
</tr>
</thead>
<tbody>
<tr>
<td>8</td>
<td>18.54</td>
<td>96.396</td>
</tr>
<tr>
<td>60</td>
<td>12.1389</td>
<td>66.013</td>
</tr>
<tr>
<td>200</td>
<td>8.375</td>
<td>29.538</td>
</tr>
</tbody>
</table>

Table 3: The trade-off between nb(SSA) and nb(nearest) for the scaling factors γ (1/2, 1/3 and 1/4), and the respective speed-up.

Table 4: Comparison of the precision between the proposed indexing method and the Kd-tree.

<table>
<thead>
<tr>
<th>k</th>
<th>8</th>
<th>30</th>
<th>60</th>
<th>100</th>
</tr>
</thead>
<tbody>
<tr>
<td>Kd-tree</td>
<td>0.953</td>
<td>0.84063</td>
<td>0.81021</td>
<td>0.75938</td>
</tr>
<tr>
<td>Lattice</td>
<td>0.938</td>
<td>0.8669</td>
<td>0.82063</td>
<td>0.7728</td>
</tr>
</tbody>
</table>

7. CONCLUSION

In this paper, we have proposed a new method for indexing a large amount of feature vectors exploiting the good properties of the algebraic lattice \( Z^n \). The proposed method performs better than the Kd-tree in both the speed-up and the precision of the retrieval process. Future works will be oriented to extract feature vectors from the most pertinent object in the images.

Appendix

Given the number \( r \), the number of parts \( d \) and the largest part \( k \), \( q(r,d,k) \) is computed by the following algorithm:

\[
q = 0_{r+1,k+1}; \quad // \text{Null Matrix of size} (r+1)\times(k+1) \\
q(0,0) = 1; \\
\text{For } i \text{ from } 0 \text{ to } d \text{ do} \\
\quad \text{For } j \text{ from } 1 \text{ to } k \text{ do} \\
\quad \quad \text{For } z \text{ from } r \text{ to } i \text{ by } -1 \text{ do} \\
\quad \quad \quad \text{If } z \geq j \text{ then} \\
\quad \quad \quad \quad q(z,j) = q(z, j-1) + q(z-j,j); \\
\quad \quad \quad \text{else} \\
\quad \quad \quad \quad q(z,j) = q(z,j-1); \\
\quad \quad \text{EndIf} \\
\quad \text{EndFor} \\
\text{EndFor} \\
\text{EndFor} \\
\text{return } q(r,d,k); 
\]

REFERENCES


