Most blind hyperspectral unmixing methods exploit convex geometry properties of hyperspectral data. The minimum volume simplex analysis (MVSA) is one of such methods which, as many others, estimates the minimum volume (MV) simplex where the measured vectors live. MVSA was conceived to circumvent the matrix factorization step often implemented by MV based algorithms and also to cope with outliers, which compromise the results produced by MV algorithms. Inspired by the recently proposed robust minimum volume estimation (RMVES) algorithm, we herein introduce the robust MVSA (RMVSA), which is a version of MVSA robust to noise. As in RMVES, the robustness is achieved by employing chance constraints, which control the volume of the resulting simplex. RMVSA differs, however, substantially from RMVES in the way optimization is carried out. The effectiveness of RMVSA is illustrated by comparing its performance in simulated data with the state-of-the-art.

Index Terms—Hyperspectral imaging, spectral unmixing, endmember identification, minimum volume simplex analysis (MVSA), chance constraints.

1. INTRODUCTION

Hyperspectral unmixing (HU) aims at estimating the number of reference substances, also called endmembers, their spectral signatures, and their abundance fractions in hyperspectral imagery [1]. In practice, hyperspectral unmixing is a source separation problem [2]. Compared with the canonical source separation scenario, the sources in hyperspectral unmixing are statistically dependent, and the observed mixture is either linear or nonlinear in nature [3]. The linear mixing model holds when the mixing scale is macroscopic [4, 5].

Linear unmixing techniques can be classified into statistical and geometrical-based [1]. The former category addresses spectral unmixing as an inference problem, often formulated under the Bayesian framework, whereas the latter category exploits the fact that the spectral vectors (under the linear mixing model) are in a simplex whose vertices correspond to the endmembers. The main research lines presented in recent years under this framework belong to two different groups: a) pure pixel based algorithms assume that the scene contains at least one pure pixel per endmember [1]; b) more recently, several algorithms dropped this assumption by assuming that no pure pixels may be present in real hyperspectral scenes [1,2,6]. In this case, a widely used strategy is to fit a simplex of minimum volume to the data set. Relevant works exploiting this direction are the minimum volume constrained non-negative matrix factorization (MVC-NMF) [7], the minimum volume simplex analysis MVSA [8], the simplex identification via split augmented Lagrangian (SISAL) algorithm [9], the minimum-volume enclosing simplex (MVES) [10], the collaborative nonnegative matrix factorization [11] (CoNMF), and the RMVES [12], among others (see [1,2] for an exhaustive account of MV based algorithms).

The MV based approach to HU is quite appealing and underlies a large number of blind HU methods introduced in the last 20 years. The simplex of MV is, however, highly sensitive to noise and outliers, what limits its applicability. Aiming at endowing the MV criterion with robustness to outliers, MVSA [8] replaces the hard abundance non-negativity constraint with a soft abundance non-negativity enforced by the hinge function. This robust to outliers version of MVSA is efficiently implemented by the SISAL [9] algorithm.

In this work, inspired by chance constraints [13] used in the RMVES, we develop a robust to noise version of MVSA (RMVSA). Although RMVSA solves the same problem as RMVES, we adopt a different optimization strategy, which turned out to be effective in terms of computational complexity and of the quality of the estimates.

The remainder of the paper is organized as follows. Section 2 describes the proposed RMVSA algorithm. Section 3 presents experiments with simulated data. A quantitative assessment to other popular endmember identification algorithms is also provided. Section 4 concludes the paper with some remarks and future research lines.
2. ROBUST MINIMUM VOLUME SIMPLEX ANALYSIS (RMVSA)

Let the data spectral vectors $Y \equiv [y_1, \ldots, y_n] \in \mathbb{R}^{p \times n}$ be a matrix holding its columns spectral vectors $y_i \in \mathbb{R}^p$, where $p$ is the number of endmembers and $n$ is the number of pixels. We assume that a dimensionality reduction step (see, e.g., [14]) was applied to the data such that the vectors $y_i \in \mathbb{R}^p$ are the coordinates of the original vectors with respect to a basis of the subspace spanned by the original measured vectors. Under the linear mixing model, we have

$$Y = MS + W,$$

s.t.:

$$S \geq 0, \quad 1_p^T S = 1_n^T,$$  \hspace{1cm} (1)

where $M \equiv [m_1, \ldots, m_p] \in \mathbb{R}^{p \times p}$ is the mixing matrix ($m_i$ denotes the $i$-th endmember signature and $p$ is the number of endmembers), and $S \in \mathbb{R}^{p \times n}$ is the abundance matrix containing the fractions of each endmember, $1_m = [1, 1, \ldots, 1]^T$ is an $m \times 1$ vector of ones, $W \equiv [w_1, \ldots, w_n]$ accounts for noise, and the notation $(\cdot)^T$ stands for vector or matrix transpose. Owing to physical constraints [15], for each pixel, the fraction vectors should be no less than zero, and sum to 1. Therefore, the spectral vectors $y_i$, belong to a simplex set with vertices $m_i$. MVSA aims at finding the matrix $M$ with minimum volume defined by its columns under the constraints in (1). As shown in [8], an equivalent formulation of this criterion in the absence of noise is as the follows:

$$\hat{Q} = \arg \max_Q \log |\det(Q)|$$

s.t.:

$$QY \geq 0, \quad 1_p^T Q = a,$$  \hspace{1cm} (2)

where $Q \equiv M^{-1}$ and $a = 1_n^T Y (YY^T)^{-1}$.

MVSA solves problem (2) using sequential quadratic programming (SQP). In addition to the criterion (2), a robust to outliers version called SISAL [9] was also introduced. In this robust version, the constraint $QY \geq 0$ is replaced with a soft constraint $-1^T \text{hinge}(-QY) 1$, where $\text{hinge}(x)$ is an element-wise operator that, for each component, yields the negative part of $x$.

From (1) we have $QY = S + QW$. When the noise is not negligible, the constraint $QY \geq 0$ act on $S + QW$ and not only on $S$, inflating the estimated simplex with respect to the true one. To mitigate this negative effect, and inspired by the RMVES method [12], we replace the constraint $QY \geq 0$ with the probability constraints $P([QY - QW]_{in} \geq \eta_i)$ for $i = 1, \ldots, p$ and $n = 1, \ldots, N$, where $P(\cdot)$ denotes probability and $[X]_{ij}$ is the $(i, j)$ component of matrix $X$.

Let $q_i$ denote the column vector formed by the $i$th row of $Q$ and assume that the noise random vectors $w_i$, for $i = 1, \ldots, N$, are Gaussian distributed with zero mean and projected covariance matrix $D_w$, where $D_w = U_p^T D U_p$. $D$ is the noise covariance matrix and $U_p$ is the affine projection matrix to $\mathbb{R}^p$. With this definition in place, we reformulate the unmixing problem using probability constraints as follows:

$$\hat{Q} = \arg \min_Q -\log |\det(Q)|$$

s.t.:

$$q_i^T y_n \geq \Phi^{-1}(\eta) \sqrt{q_i^T D_w q_i},$$

$$1_p^T Q = a, \ \forall i \in \{1, \ldots, p\}, \ \forall n \in \{1, \ldots, N\},$$  \hspace{1cm} (3)

where $\Phi(\cdot)$ denotes the cumulative distribution function of the standard normal random variable (Gaussian random variable with zero mean and unit variance).

From (3), it can be inferred that, when $\eta = 0.5$, $\Phi^{-1}(\eta) = 0$ and (3) is equivalent to MVSA under hard constraints. When $\eta < 0.5$, $\Phi^{-1}(\eta) < 0$, the terms $q_i y_n$ may take negative values meaning that the RMVSA solution approaches the real simplex. This scenario is illustrated in Fig. 1.

The optimization problem (3) is difficult since the objective function is nonconvex and the constraints are nonlinear and, if $\eta < 0.5$, nonconvex. In this work, we propose a relaxation of the inequality constraint which can be defined as follows. At the $t + 1$ iteration, we have

$$Q^{(t+1)} = \arg \min_Q -\log |\det(Q)|$$

s.t.:

$$q_i^T y_n \geq \Phi^{-1}(\eta) \sqrt{q_i^T D_w q_i},$$

$$1_p^T Q = a, \ \forall i \in \{1, \ldots, p\}, \ \forall n \in \{1, \ldots, N\},$$  \hspace{1cm} (4)

where $q_i$ is the $i$th row of $Q^{(t+1)}$. The advantage of (4) is that the constraints are linear and, thus, we may still apply the SQP based approach used in the original MVSA [8]. In the following we will briefly describe the MVSA algorithm [8] and its modification aimed at solving the optimization (4).

Denote $q \equiv \text{vec}(Q)$, i.e., the columnwise stacking of the columns of $Q$ and define $f(q) \equiv -\log |\det(Q)|$. We adopt the majorization minimization strategy to solve (4), which amounts to iteratively minimize a majorizer of $f$, denoted as $\phi(q; q^{(t)})$, such that $\phi(q^{(t)}; q^{(t)}) = f(q^{(t)})$, $\phi(q; q^{(t)}) \geq f(q^{(t)})$, and $\phi(q, q^{(t)})$ is easy to minimize. Using the fact that the gradient and the Hessian of $f$ are, respectively, given by $g(q) = \text{vec}(-Q^{-T})$ and $H(q) = K_n [Q^{-T} \otimes Q^{-1}]$, where $K_n$ is the commutation matrix (i.e., $K_n \text{vec}(A) = \text{vec}(A^T)$) (see [9] for details), we define the following local majorizer for $f$:

$$\phi(q; q^{(t)}) \equiv \beta^{(t)} + c^{(t)}^T q + \frac{1}{2} q^T G^{(t)} q$$  \hspace{1cm} (5)

where $c^{(t)} = g(q^{(t)}) - H(q^{(t)}) q^{(t)}$ and $G^{(t)} = \text{diag}(H(q^{(t)}))$.

Define $A_I = Y^T \otimes I_p$, $A_E = I_p \otimes 1_p$, $b_I^{(t)} = \text{vec}((\Phi^{-1}(\eta) \sqrt{q_i^T D_w q_i})^T)$, and $b_E = a$, where $\otimes$ is the Kronecker product and $I_p$ is the identity matrix. Therefore, the minimization of (5) subject to the constraints shown in (4) may be written compactly as

$$\min \ \phi(q; q^{(t)}) = c^{(t)}^T q + \frac{1}{2} q^T G^{(t)} q$$

s.t.:

$$A_I q \geq b_I^{(t)}, \quad A_E q = b_E,$$  \hspace{1cm} (6)
which is a quadratic programming (QP) problem. Algorithm 1 shows the proposed SQP RMVSA algorithm.

**Algorithm 1 RMVSA pseudocode**

1. **INPUT**: $A_I$, $A_E$, $b_E$, $q_0$, where $q_0$ an initial solution
2. **COMMENT**: $f(q) = -\log |\det(Q)|$ is the objective function
3. $\text{Convergence} \leftarrow false$, $\text{Iterations} \leftarrow 0$, $q = q_0$
4. **repeat**
5. Compute $c$, $G$, and $b_I$ (defined after (5))
6. $q \leftarrow$ solution of the quadratic optimization (6)
7. **if** $f(q_0) < f(q)$ **then**
8. //Take the middle of $q_0$, $q$
9. **end if**
10. **if** $|f(q_0) − f(q)| < \text{threshold}$ **then**
11. $\text{Convergence} \leftarrow true$
12. **end if**
13. $q_0 \leftarrow q$
14. $\text{Iterations} \leftarrow \text{Iterations} + 1$
15. **until** $\text{Convergence or Iterations} \geq 4$

As discussed in [1], a major issue for a MV algorithm is that it is not strictly convex or concave, thus a proper initialization is very important. In this work, we use the MVSA solution as an initialization for RMVSA. MVSA can be executed by the same algorithm by setting $b_I = 0$. Another important issue for Algorithm 1 is its convergence. Although we still do not have a proof convergence, we have systematically observed that a maximum of 4 iterations were sufficient for RMVSA to converge.

![Endmembers and data points (2D projection)](image)

**Fig. 1.** Plot of the endmember simplex for $\eta < 0.5$, $\eta = 0.5$ and $\eta > 0.5$

3. EXPERIMENTS

In this section we compare the RMVSA algorithm presented in this work with other state of the art algorithms for endmember extraction, specifically RMVES [12], MVSA [8], MVES [10] and N-FINDR [16]. For a given data set, all algorithms were run just once whereas, owing to its sensitivity to the initialization, RMVES was run 10 times with $\Phi^{-1}(\eta) = -0.3$ taking the best result as explicitly suggested by its Authors. To evaluate the performance of the different algorithms, the estimated abundance fractions ($\hat{A}$) generated by inverse constrained minimization, and the signature estimates ($\hat{M}$) are compared with the true ones ($A$ and $M$, respectively). Both $A$ and $\hat{A}$ are acquired by the inverse minimization process using $M$ and $\hat{M}$ respectively. We use several metrics to evaluate the proposed approach. The first one is the mean square error (MSE), denoted as $\| e \|_F = \| M - \hat{M} \|_F$ where $\| \cdot \|_F$ stands for the Frobenius norm. Another metric considered in our experiments is the reconstruction error, computed as $r_{\epsilon} = \| \hat{Y} - Y \|_F = \| MA - Y \|_F$. The third metric used in this work is the spectral angle distance (SAD) (in degrees) expressed as $\text{SAD} = \cos^{-1}\left(\frac{\hat{m}_i^T m_i}{\|\hat{m}_i\| \|m_i\|}\right)$ [3]. All algorithms have been implemented in Matlab.

Our experiments have been conducted on a synthetic image of size $100 \times 100$ pixels and 200 bands. The spectral signatures are random uniform and selected from the USGS library [17] and are used to construct the data-sets under the linear mixture model (1). The data are Dirichlet distributed and uniformly distributed over the simplex. Zero-mean white Gaussian noise, defined as $\text{SNR} = 10\log_{10}\left(\frac{\text{E}[Y_i^2]}{\text{E}[W_i^2]}\right)$ (dB), has been added to the synthetic scene. We distinguish two cases, first when pure pixels exist, second when non pure pixels exist in the synthetic image.

3.1. Pure pixel based experiments

In the first experiment, we evaluate the proposed RMVSA algorithm by assuming that pure pixels are present in the considered data set, simulated with $p = 5$ endmembers. Tables 1 and 2 show the results obtained by the aforementioned methods for the considered scene with different noise levels. It can be observed that both RMVSA and RMVES perform better than their corresponding hard constrained versions of MVSA and RMVES, respectively. RMVSA performs slightly better than RMVES due to the fine tuning of the probability parameter. Both RMVES and RMVSA manage to achieve similar results as N-FINDR which is not the case for MVSA and MVES which is their major weakness.

3.2. Non pure pixel based experiments

In this subsection, we evaluate RMVSA by assuming that no pure pixels exist in the considered image (the maximum purity is 0.8). The same experimental set was constructed as with the previously experiment. Tables 3 and 4 show the obtained results from the same methods for the considered
Table 1. Comparison of endmember extraction algorithms on a synthetic image containing pure mineral signatures from the USGS library under different noise levels.

| dB  | RMVSA $\parallel \epsilon \parallel_F^{\infty}$ r$\epsilon$ SAD $|\Phi^{-1}(\eta)|$ | RMVES $\parallel \epsilon \parallel_F^{\infty}$ r$\epsilon$ SAD | MVSA $\parallel \epsilon \parallel_F^{\infty}$ r$\epsilon$ SAD | MVES $\parallel \epsilon \parallel_F^{\infty}$ r$\epsilon$ SAD | N-FINDR $\parallel \epsilon \parallel_F^{\infty}$ r$\epsilon$ SAD |
|-----|---------------------------------|-----------------|-----------------|-----------------|-----------------|
| 40  | 0.004 6.4e-6 0.2 0.05 0.13 4.3e-5 0.6 | 0.007 6.4e-6 0.4 | 0.009 6.4e-6 0.5 | 0.002 7.8e-6 0.6 |
| 30  | 0.01 2e-5 0.5 0.07 0.04 3.7e-5 2.1 | 0.02 2e-5 1.3 | 0.13 2e-5 3.5 | 0.003 2.5e-5 1.9 |
| 20  | 0.02 6.5e-5 1.3 0.08 0.03 6.8e-5 2.2 | 0.12 6.5e-5 5.1 | 0.12 6.5e-5 5 | 0.01 8.3e-5 6.3 |
| 10  | 0.06 2.1e-04 3 0.1 0.07 2.1e-04 3.3 | 0.99 2.1e-4 18.8 | 0.94 2.1e-4 18.1 | 0.04 2.5e-04 18.3 |

Table 2. Comparison of endmember extraction algorithms on a synthetic image containing random, uniformly distributed, pure pixels under different noise levels.

| dB  | RMVSA $\parallel \epsilon \parallel_F^{\infty}$ r$\epsilon$ SAD $|\Phi^{-1}(\eta)|$ | RMVES $\parallel \epsilon \parallel_F^{\infty}$ r$\epsilon$ SAD | MVSA $\parallel \epsilon \parallel_F^{\infty}$ r$\epsilon$ SAD | MVES $\parallel \epsilon \parallel_F^{\infty}$ r$\epsilon$ SAD | N-FINDR $\parallel \epsilon \parallel_F^{\infty}$ r$\epsilon$ SAD |
|-----|---------------------------------|-----------------|-----------------|-----------------|-----------------|
| 40  | 0.001 8.9e-6 0.1 0.02 0.004 9e-6 0.23 | 0.004 8.9e-6 0.22 | 0.006 8.9e-6 0.3 | 0.001 1.1e-5 0.5 |
| 30  | 0.006 2.8e-5 0.3 0.03 0.018 3.45e-5 0.7 | 0.02 2.8e-5 0.8 | 0.13 2.8e-5 3 | 0.005 3.4e-5 1.6 |
| 20  | 0.02 8.8e-5 1 0.04 0.03 8.8e-5 1.4 | 0.06 8.8e-5 3 | 0.07 8.8e-5 3.3 | 0.02 1.1e-4 5.1 |
| 10  | 0.04 2.7e-4 2 0.04 0.06 2.8e-4 3 | 0.21 2.7e-4 9.8 | 0.24 2.8e-4 10.7 | 0.04 3.3e-4 15.6 |

Table 5. Processing time (seconds) obtained on a synthetic image for different number of endmembers.

<table>
<thead>
<tr>
<th>$p$</th>
<th>RMVSA</th>
<th>RMVES</th>
<th>MVSA</th>
<th>MVES</th>
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<tr>
<td>5</td>
<td>4.1</td>
<td>29.7</td>
<td>2.4</td>
<td>15.3</td>
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<tr>
<td>10</td>
<td>42.9</td>
<td>1788</td>
<td>22.9</td>
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3.3. Computational complexity

In this subsection we present the processing times of RMVSA (including initialization), RMVES, MVSA, MVES on a synthetic image of $100 \times 100$ image with SNR = 30dB for different number of end-members. The times (in secs) were measured in a 4-core desktop PC at 3.0 GHz and 8 GB of RAM. In Table 5 it can be observed that RMVSA takes twice the time of MVSA and takes significant less time than RMVES.

4. CONCLUSIONS AND FUTURE LINES

In this work, we have introduced a new robust minimum volume simplex analysis (RMVSA) algorithm for HU. By including chance constraints, the proposed RMVSA is able to deal with scenarios in which noise exist. An important contribution of this work is the relaxation of the chance constraint, such that the constraints of the optimization problem are linear. This brings great advantages from both the theoretical and computational viewpoints. The proposed RMVSA algorithm was evaluated using different simulated hyperspectral data sets, in comparison with other state of the art minimum volume based algorithms. The experimental results showed that the proposed algorithm is very efficient for unmixing highly mixed and noisy data. Future work will focus on evaluating the proposed methodology using real data and on providing theoretical values for the $\eta$ parameter based on the distribution of the data. We will also search for a theoretical upper bound for the number of iterations needed for convergence of the proposed optimization.

Acknowledgement

We would like to gratefully thank the Authors of RMVES for their kind advices on how to properly run RMVES.

REFERENCES

Table 3. Comparison of endmember extraction algorithms on a synthetic image containing non pure mineral signatures from the USGS library under different noise levels.

<table>
<thead>
<tr>
<th>dB</th>
<th>( | \epsilon |_F )</th>
<th>re</th>
<th>SAD</th>
<th>( \Phi^{-1}(\eta) )</th>
<th>( | \epsilon |_F )</th>
<th>re</th>
<th>SAD</th>
<th>( | \epsilon |_F )</th>
<th>re</th>
<th>SAD</th>
<th>( | \epsilon |_F )</th>
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Table 4. Comparison of endmember extraction algorithms on a synthetic image containing random, uniformly distributed, non pure pixels under different noise levels.

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<th>dB</th>
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<th>re</th>
<th>SAD</th>
<th>( \Phi^{-1}(\eta) )</th>
<th>( | \epsilon |_F )</th>
<th>re</th>
<th>SAD</th>
<th>( | \epsilon |_F )</th>
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